

## Year 12 / AS

## Weekly Tutorial 02

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- 1. Find the values of k such that the equation  $k = kx^2 3x + 2k = 0$  has no real roots.
- 2.  $x^2 2(a+1)x + 3a = 0$ Describe the nature of roots of above quadratic equation for different values of a.
- 3. Find the range of values of k such that,  $2x^2 - 4x + (3k - 2) > 0$
- 4. Find the range of values of k such that,  $3x^2 2(k+2)x + 3 = 0$  has real roots.
- 5. Simplify the following.

a) 
$$\left(4x^{12} + \frac{17x^{12}}{27}\right)^{-\frac{2}{3}}$$

**b)** 
$$a^2 \left(3a^{-\frac{1}{4}}\right)^4$$

6. Solve.

a) 
$$2x^2 - (2\sqrt{3} + 3)x + 3\sqrt{3} > 0$$

**b)** 
$$x^2 + 3x - 1 \le 0$$

7.

- a) Write  $x^2 + 5x + 15$  in the form  $(x + a)^2 + b$ . Where a and b are real constants.
- **b)** Hence, or otherwise find the maximum value of  $\frac{1}{x^2+5x+15}$
- 8.  $f(x) = -3x^2 + 2x + 30$ Find the minimum value of  $\frac{5}{f(x)}$ .